

AG1: Solve in \mathbb{R}^2 system of two quadratic equations with two unknowns:

$$x^2 + 0.25y^2 = 1; \quad 0.25x^2 + y^2 = 1$$

$$\left[\pm \frac{\sqrt{5}}{5}, \frac{\sqrt{5}}{5} \right], \left[\pm \frac{\sqrt{5}}{5}, -\frac{\sqrt{5}}{5} \right]$$

AG2: Solve in \mathbb{R}^2 system of two quadratic equations with two unknowns:

$$x^2 + xy + y^2 = 9; \quad x^2 + xy - y^2 = 1$$

$$\left[-1 \pm \sqrt{6}, 2 \right], \left[1 \pm \sqrt{6}, -2 \right]$$

AG3: Solve in \mathbb{R}^2 system of two quadratic equations with two unknowns:

$$x^2 + y = 2; \quad 2x^2 + 2x + y = 1$$

$$[-1, 1]$$

AG4: Curves are determined by implicit and parametric equations. Determine the intersection points to two decimal places of precision.

$$x^2 + y = 2; \quad X(t) = [2 \cdot \cos(t), 2 \cdot \sin(t)]$$

$$T = [0, 2] \quad C_{12} = [\pm\sqrt{3}, -1]$$

AG5: Conics are determined by implicit and parametric equations. Determine the intersection points to two decimal places of precision.

$$xy = 1; \quad X(t) = [\cosh(t), \sinh(t)]$$

$$[1.27; 0.79]$$

AG6: Determine foci and vertices of conic $xy + x = 1$ to two decimal points of precision.

$$A=[1,0]; B=[-1,-2], F_{1,2} = [\pm\sqrt{2}, \pm\sqrt{2} - 1]$$

AG7: Determine the intersection points of ellipse $X(t) = [5 \cos(t), \sqrt{5} \sin(t)]$ and straight line AB, where $A = [-2, 0]$, $B = [0, 1]$.

$$[-4.29, -1.15], [2.07, 2.04]$$

AG8: Write the parametric equations of ellipse with center $C = (2, 3)$ semi-major axis $a = 5$ and linear eccentricity $e = 4$.

$$[5 \cos t + 2, 3 \sin t + 3]$$

Tangent line to a conic is a line that touches the conic at exactly one point, never entering the conic's interior. Roughly speaking, it is a line through a pair of infinitely close points on the conic.

AG9: Determine the tangent line of hyperbola $X(t) = [\cosh(t), \sinh(t)]$ from an exterior point $M = (0, 1)$.

$$\pm y = \mp \sqrt{2} + 1$$

AG10: Determine the tangent line of a circle $X(t) = [\cos(t), \sin(t)]$ from a given point $M = (1, 1)$.

$$y = 1, x = 1$$